

1. Consider the following experiment:  
A letter is chosen at random from the word **STATISTICS**.
  - a) List all possible outcomes and their probabilities.
  - b) What is the probability that the letter selected is a vowel?
  
2. If  $P(A) = 0.7$ ,  $P(B) = 0.5$ , and  $P(A' \cap B') = 0.1$ , find ...
  - a)  $P(A \cap B)$ ;
  - b)  $P(A | B)$ ;
  - c)  $P(B | A)$ .
  
3. Suppose  $P(B) = 0.45$ ,  $P(A \cup B) = 0.67$ ,  $P(A \cup B') = 0.89$ . Find ...
  - a)  $P(A)$ .
  - b)  $P(A | B')$ .
  - c)  $P(B' | A')$ .
  
4. a) **1.1-7**      **1.2-9**  
Given that  $P(A \cup B) = 0.76$  and  $P(A \cup B') = 0.87$ , find  $P(A)$ .
  - b) Suppose also that  $P(B) = 0.20$ . Find ...
    - i)  $P(A \cap B)$ ;
    - ii)  $P(A | B)$ ;
    - iii)  $P(B | A)$ .

5. **1.2-16** 1.2-14

The five numbers 1, 2, 3, 4, and 5 are written respectively on five disks of the same size and placed in a hat. Two disks are drawn without replacement from the hat, and the numbers written on them are observed.

- a) List the 10 possible outcomes of this experiment as unordered pairs of numbers.
- b) If each of the 10 outcomes has probability  $1/10$ , assign a value to the probability that the sum of the two numbers drawn is
  - (i) 3;
  - (ii) between 6 and 8 inclusive.

6. A bank classifies borrowers as "high risk" or "low risk," and 16% of its loans are made to those in the "high risk" category. Of all the bank's loans, 5% are in default. It is also known that 40% of the loans in default are to high-risk borrowers.

- a) What is the probability that a randomly selected loan is in default and issued to a high-risk borrower?
- b) What is the probability that a loan will default, given that it is issued to a high-risk borrower?
- c) What is the probability that a randomly selected loan is either in default or issued to a high-risk borrower, or both?
- d) A loan is being issued to a borrower who is not high-risk. What is the probability that this loan will default?

7. At *Initech*, 60% of all employees surf the Internet during work hours. 24% of the employees surf the Internet and play MMORPG during work hours. It is also known that 72% of the employees either surf the Internet or play MMORPG (or both) during work hours.

- a) What proportion of the employees play MMORPG during work hours?
- b) If it is known that an employee surfs the Internet during work hours, what is the probability that he/she also plays MMORPG?
- c) Suppose an employee does not play MMORPG during work hours. What is the probability that he/she surfs the Internet?

8. Suppose  $S = \{1, 2, 3, \dots\}$  and  $P(x) = \left(\frac{1}{2}\right)^x$ ,  $x = 1, 2, 3, \dots$ .

- a) Find  $P(\text{outcome is divisible by } 3)$ .
- b) Find  $P(\text{outcome is divisible by } 3 \mid \text{outcome is divisible by } 2)$ .

9. 500 people, all of whom drive approximately 10,000 miles per year, were classified according to age and the number of auto accidents each has had during the last three years:

<i>Number of Accidents</i>	<i>Age (in years)</i>	
	<b>Under 40</b>	<b>Over 40</b>
<b>0</b>	170	80
<b>1</b>	80	70
<b>More than 1</b>	50	50

A person is selected at random from those 500.

- a) What is the probability that the person selected is over 40 and has had more than 1 accident?
- b) What is the probability that the person selected is either over 40 or has had more than 1 accident (or both)?
- c) Find the probability that the person selected is over 40 given that he/she has had more than 1 accident.
- d) Suppose that the person selected is over 40. What is the probability that he/she has had more than 1 accident?
- e) Find the probability that the person selected is over 40 given that he/she has had at most 1 accident.
- f) Find the probability that the person selected has had more than 1 accident given that he/she has had at least one accident.

10. **1.3-4 (c)** **1.4-4 (c)**

Two cards are drawn successively and without replacement from an ordinary deck of playing cards. Compute the probability of drawing a heart on the first draw and an ace on the second draw.

Hint: Note that a heart can be drawn by getting the ace of hearts or one of the other 12 hearts.

11. **1.3-7** **1.4-9** 1.4-9

An urn contains four colored balls: two orange and two blue. Two balls are selected at random without replacement, and you are told that at least one of them is orange. What is the probability that the other ball is also orange?

Hint 1:      O O              O B              B O              B B

Hint 2:       $P(\text{both orange} \mid \text{at least one orange})$ .

12. Bowl A contains three red and two white chips, and bowl B contains four red and three white chips. A chip is drawn at random from bowl A and transferred to bowl B.

a) **1.3-16** **1.4-18**

Compute the probability of then drawing a red chip from bowl B.

b) If a red chip was drawn from bowl B, what is the probability that a red chip had been drawn from bowl A?